



Introduction to **Neutron imaging**

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Science. Ingenuity. Sustainability.

Outline

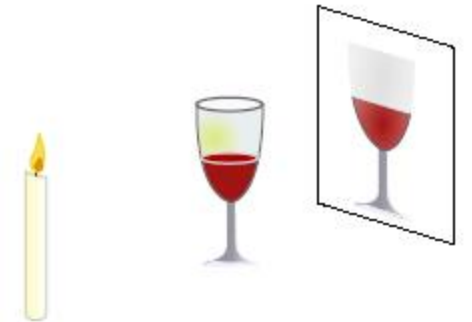
- Introduction to the method
- How image is formed
- Computed tomography
- Instrument components
- Case studies



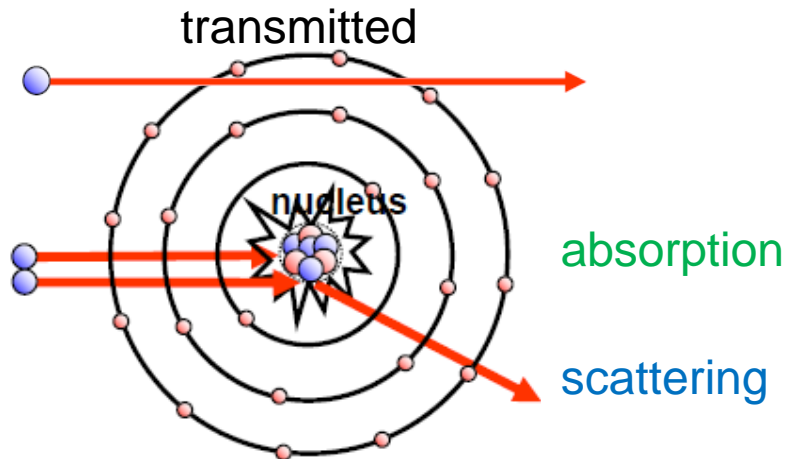
What is imaging?

We have a solid item to investigate

1. Take a first look of the outside
2. Use a transmission image
3. Cut the item in pieces ... virtually



Interaction with matter



Neutron imaging techniques

Radiography

Tomography

Real-time imaging

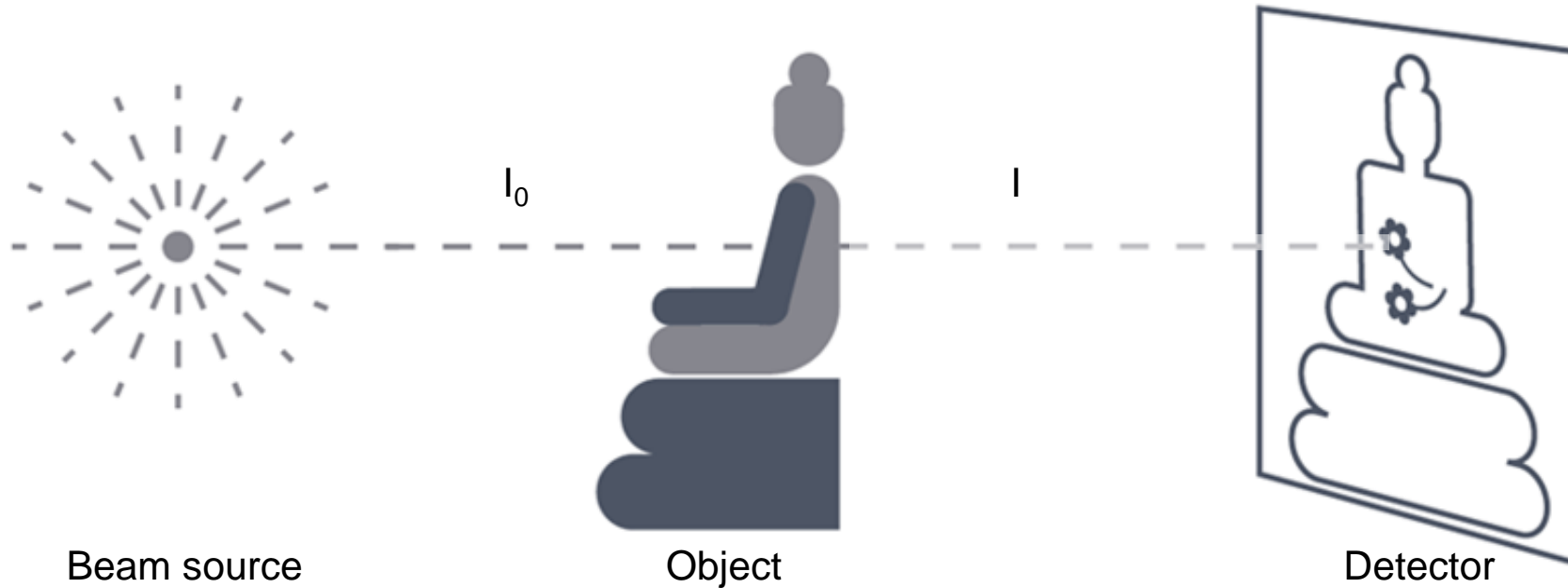
Stroboscopic imaging

Resonance capture analysis

Energy-selective imaging

Grating interferometry

Transmission Image



Beer-Lambert law

$$I(\lambda) = I_0(\lambda)e^{-\sum_i(\mu(\lambda)d)_i}$$

$I(\lambda)$ - transmitted intensity of a monochromatic beam

$I_0(\lambda)$ - incident intensity

d - path length

$\mu(\lambda)$ - total linear attenuation coefficient

$$\mu(\lambda) = \sigma_t(\lambda) \frac{\rho N_A}{M}$$

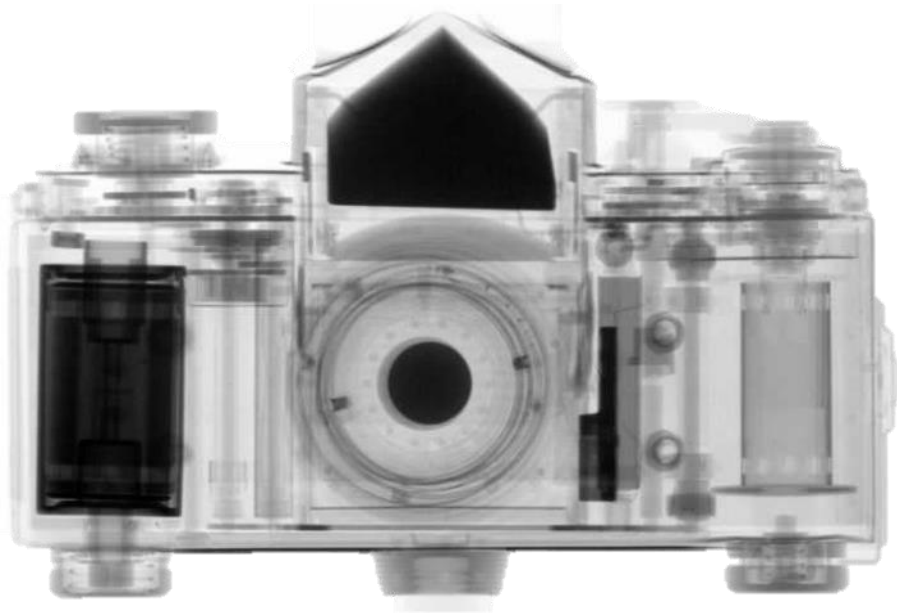
$\sigma_t(\lambda)$ - total cross-section

ρ - density

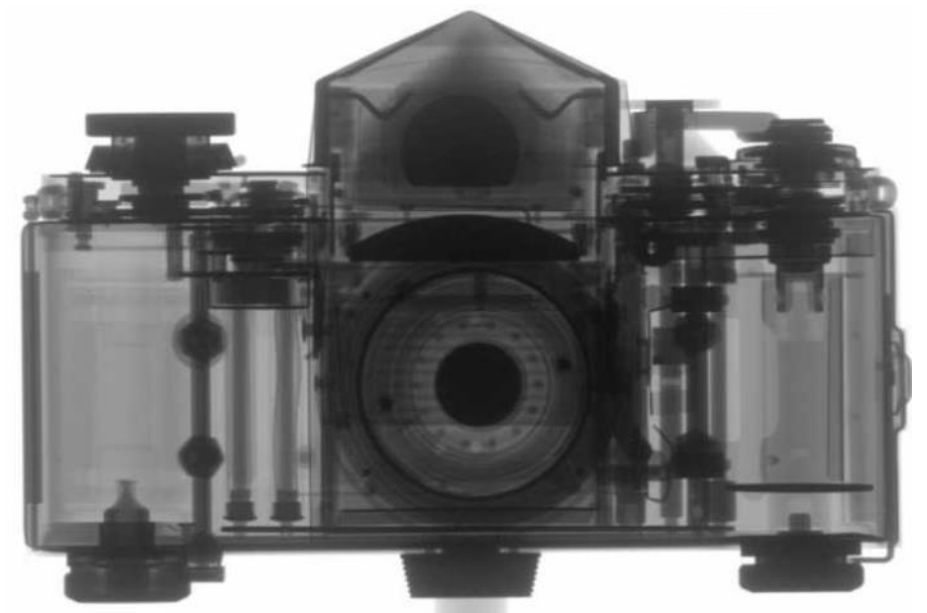
N_A - Avogadro's number

M - atomic mass

Neutrons vs X-ray



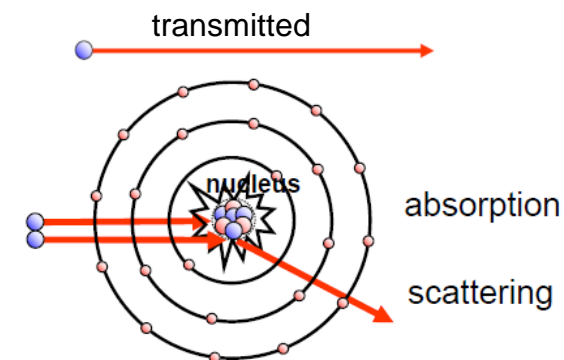
Neutrons



X-ray

Neutrons

1a	2a	3b	4b	5b	6b	7b	8	1b	2b	3a	4a	5a	6a	7a	0		
H															He		
3.44															0.02		
Li	Be									B	C	N	O	F	Ne		
3.30	0.79									101.60	0.56	0.43	0.17	0.20	0.10		
Na	Mg									Al	Si	P	S	Cl	Ar		
0.09	0.15									0.10	0.11	0.12	0.06	1.33	0.03		
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
0.06	0.08	2.00	0.60	0.72	0.54	1.21	1.19	3.92	2.05	1.07	0.35	0.49	0.47	0.67	0.73	0.24	0.61
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
0.08	0.14	0.27	0.29	0.40	0.52	1.76	0.58	10.88	0.78	4.04	115.11	7.58	0.21	0.30	0.25	0.23	0.43
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
0.29	0.07	0.52	4.99	1.49	1.47	6.85	2.24	30.46	1.46	6.23	16.21	0.47	0.38	0.27			
Fr	Ra	Ac	Rf	Ha													
	0.34																
	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu			
Lanthanides	0.14	0.41	1.87	5.72	171.47	94.58	1479.04	0.93	32.42	2.25	5.48	3.53	1.40	2.75			
	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr			
Actinides	0.59	8.46	0.82	9.80	50.20	2.86											



Pros

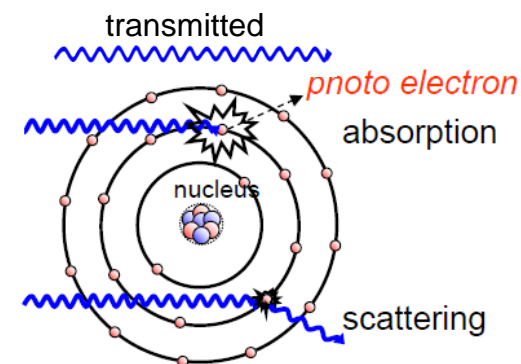
- High penetration power
- High sensitivity to H
- Non-invasive method

Cons

- Acquisition time
- Resolution
- Post-experiment radioactivity

X-ray

1a	2a	3b	4b	5b	6b	7b	8	1b	2b	3a	4a	5a	6a	7a	0		
H															He		
0.02															0.02		
Li	Be									B	C	N	O	F	Ne		
0.06	0.22									0.28	0.27	0.11	0.16	0.14	0.17		
Na	Mg									Al	Si	P	S	Cl	Ar		
0.13	0.24									0.38	0.33	0.25	0.30	0.23	0.20		
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
0.14	0.26	0.48	0.73	1.04	1.29	1.32	1.57	1.78	1.96	1.97	1.64	1.42	1.33	1.50	1.23	0.90	0.73
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
0.47	0.86	1.61	2.47	3.43	4.29	5.06	5.71	6.08	6.13	5.67	4.84	4.31	3.98	4.28	4.06	3.45	2.53
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
1.42	2.73	5.04	19.70	25.47	30.49	34.47	37.92	39.01	38.61	35.94	25.88	23.23	22.81	20.28	20.22		9.77
Fr	Ra	Ac	Rf	Ha													
	11.80	24.47															
	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu			
Lanthanides	5.79	6.23	6.46	7.33	7.68	5.66	8.69	9.46	10.17	10.91	11.70	12.49	9.32	14.07			
	Th	Pa	U	Np	Pu	Am	Cm	Bk	Vf	Es	Fm	Md	No	Lr			
Actinides	28.95	39.65	49.08														



Pros

- Fast acquisition
- High resolution
- No after-radiation

Cons

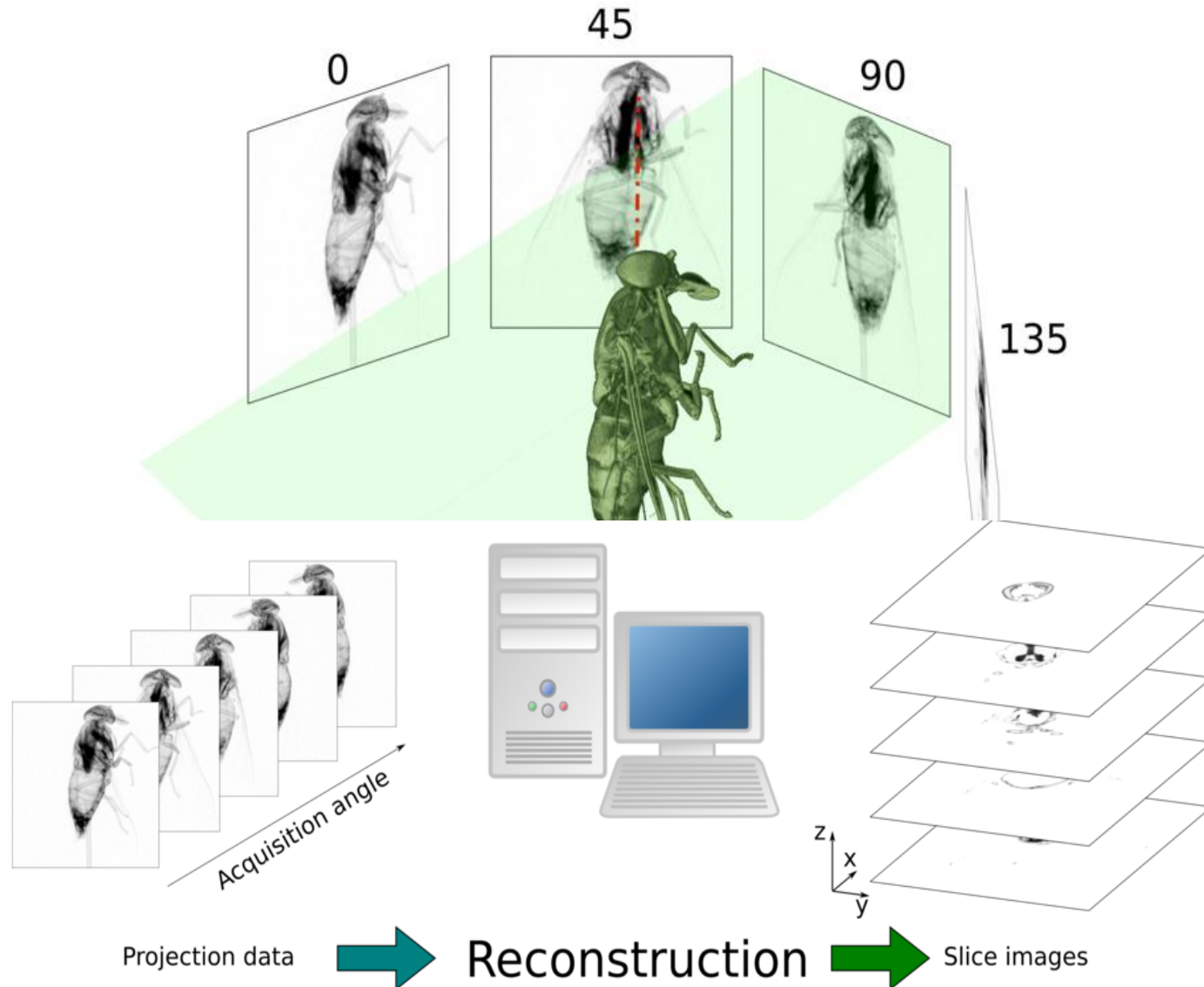
- High Z materials
- Lower material differentiation

Computed Tomography



Credit: <https://www.psi.ch/media/x-ray-and-neutron-imaging-for-palaeontologists-and-archaeologists>

Computed Tomography



Computing a transmission Image

Beer-Lambert law for each pixel of the 2D detector

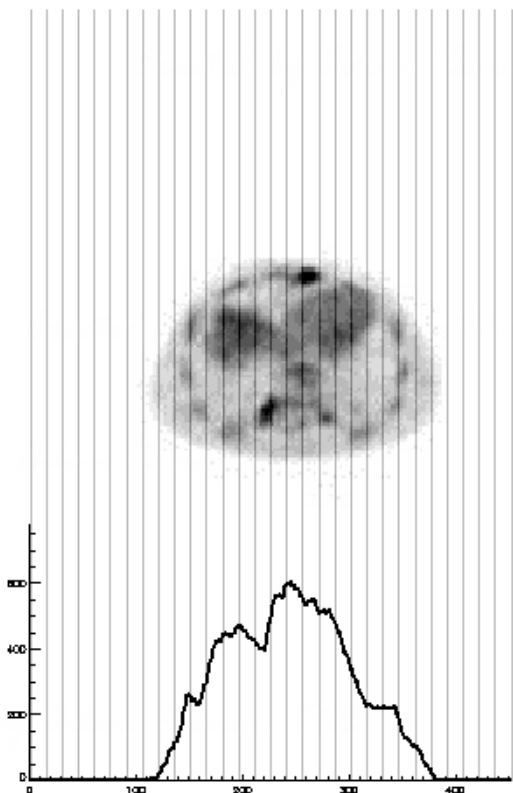
The diagram shows the process of computing a transmission image (T) from measured intensity (I) and incident beam intensity (I₀), both corrected for camera intensity offset (DC). The measured intensity (I) and incident beam intensity (I₀) are shown as grayscale images of a butterfly-like object. The camera intensity offset (DC) is shown as a black image. The transmission image (T) is the result of the subtraction of DC from I and I₀, and the division of the result by I₀ - DC.

$$T = \frac{I - DC}{I_0 - DC} = e^{-\sum_i (\mu(\lambda) d)_i}$$

Eliminate incident beam intensity variation (I_0) and camera intensity offset (DC) to get transmission image (T)

Image reconstruction: The Radon Transform and the sinogram

(True) Emission Volume

Forward
Projectionangle
0

Theta (angle)

Sinogram (stored data)

Rho (offset)

Approximations:

- Parallel and monoenergetic beam
- Interactions outside the sample and scattered neutrons are not taken into account.

The Radon transform of the one-dimensional projections $P_\theta(t)$ of single slices at angles θ can be formulated as

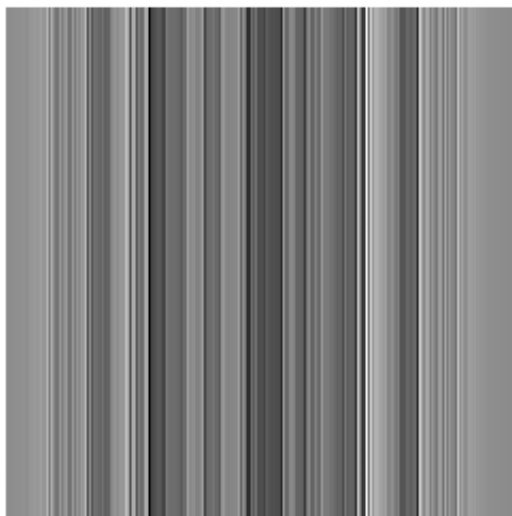
$$P_\theta(t) = -\ln \frac{I_\theta(t)}{I_0(t)} = \int_{\text{ray}(\theta,t)} \mu(x, y) \cdot ds$$

$$= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \delta_D(x \cos \theta + y \sin \theta - t) \times \mu(x, y) \cdot dx dy,$$

where $t = x \cos \theta + y \sin \theta$ and is perpendicular to the rotation axis.

Filtered-back projection Radon transform

Reconstructed image



Sinogram



← Filtered Back Projection

Rho (offset)

The **Fourier slice theorem** states that the one-dimensional Fourier transform $P_\theta(\omega)$ of the projections $P_\theta(t)$ of the two-dimensional function $\mu(x, y)$ is equal to the two-dimensional Fourier transform $S(u, v)$ of the slice $\mu(x, y)$. Consequently, an infinite number of projections will fill the whole Fourier space and enable a perfect reconstruction of $\mu(x, y)$ by the back transformation

$$\begin{aligned}\mu(x, y) &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} S(u, v) \cdot e^{2\pi i(ux+vy)} \cdot du \, dv \\ &= \int_0^\pi \int_0^\infty \left(\int_{-\infty}^{\infty} P_\theta(t) \cdot e^{-2\pi i\omega t} \cdot dt \right) \\ &\quad \times e^{2\pi i(x \cos \theta + y \sin \theta)} \cdot |\omega| \cdot d\omega \, d\theta,\end{aligned}$$

where $|\omega|$ results from the transformation into polar coordinates (u, v) .

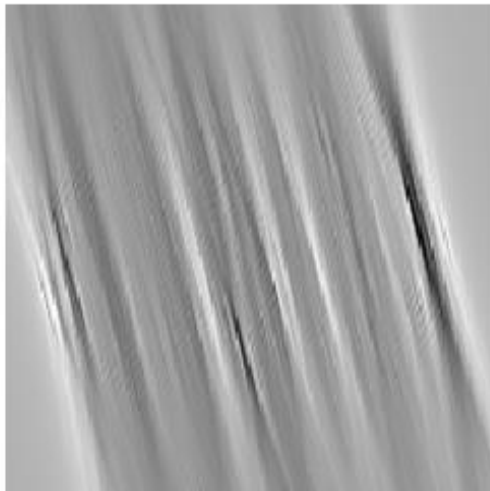
$$Q_\theta(t) = \int_0^\infty P_\theta(\omega) \cdot e^{2\pi i(x \cos \theta + y \sin \theta)} |\omega| \cdot d\omega$$

This function is called a filtered projection where $|\omega|$ can be considered to be a ramp filter.

How many projections are needed?

The number of projections is determined by the **Nyquist–Shannon sampling theorem**

Reconstructed image



Percent
backprojected
5 %
from selected
angles

Sinogram



Theta (angle)

Rho (offset)

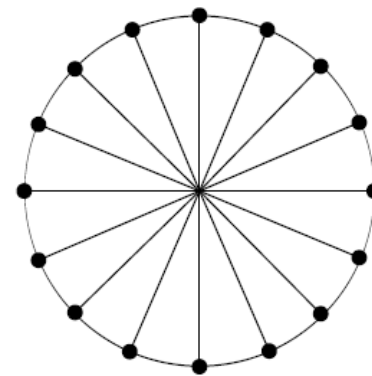
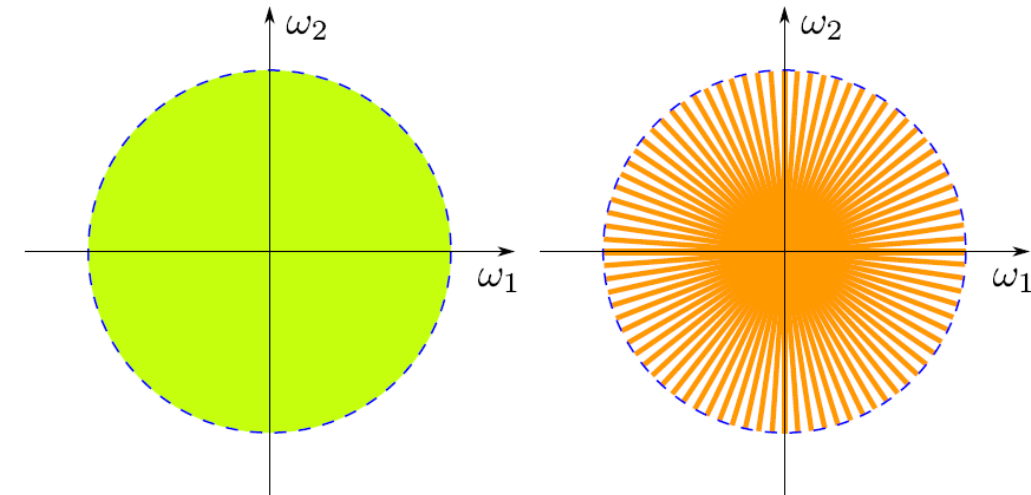
$$N = \frac{\pi}{2} M$$

N= number of projections
M=Number of pixels in the
direction perpendicular to the
axis of rotation

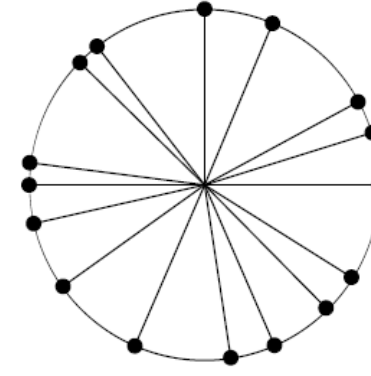
← Filtered Back Projection

When the analytical solution has problem

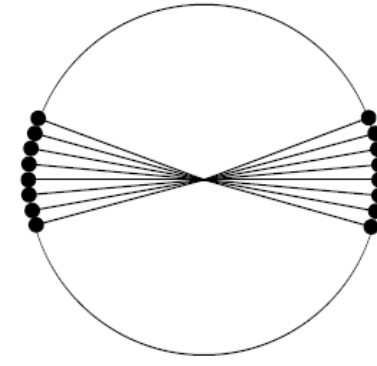
The unit circle in the Fourier domain must be filled



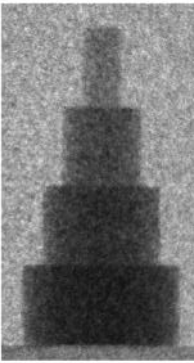
Few projections



Irregularly distributed



Limited view



Low SNR

Iterative methods

Pros

- Sparse, irregular, sampled projection data
- Physical model can be included

Cons

- Require *a priori* knowledge for best performance
- Time consuming

Image processing



Software for data reconstruction and analysis

Preliminary data treatment and filtering

ImageJ

FIJI

MATLAB – Image processing toolbox

ImageMagick

Tomographic reconstruction

Octopus

X-tract

MATLAB – Image processing toolbox

Exploring free-software i.e. *MuhRec*, *iMARS*, *CTAS*

Visualization and analysis

VG Studio MAX

Drishti

AVIZO (FEI)

Slicer3D

ParaView

Instrument components

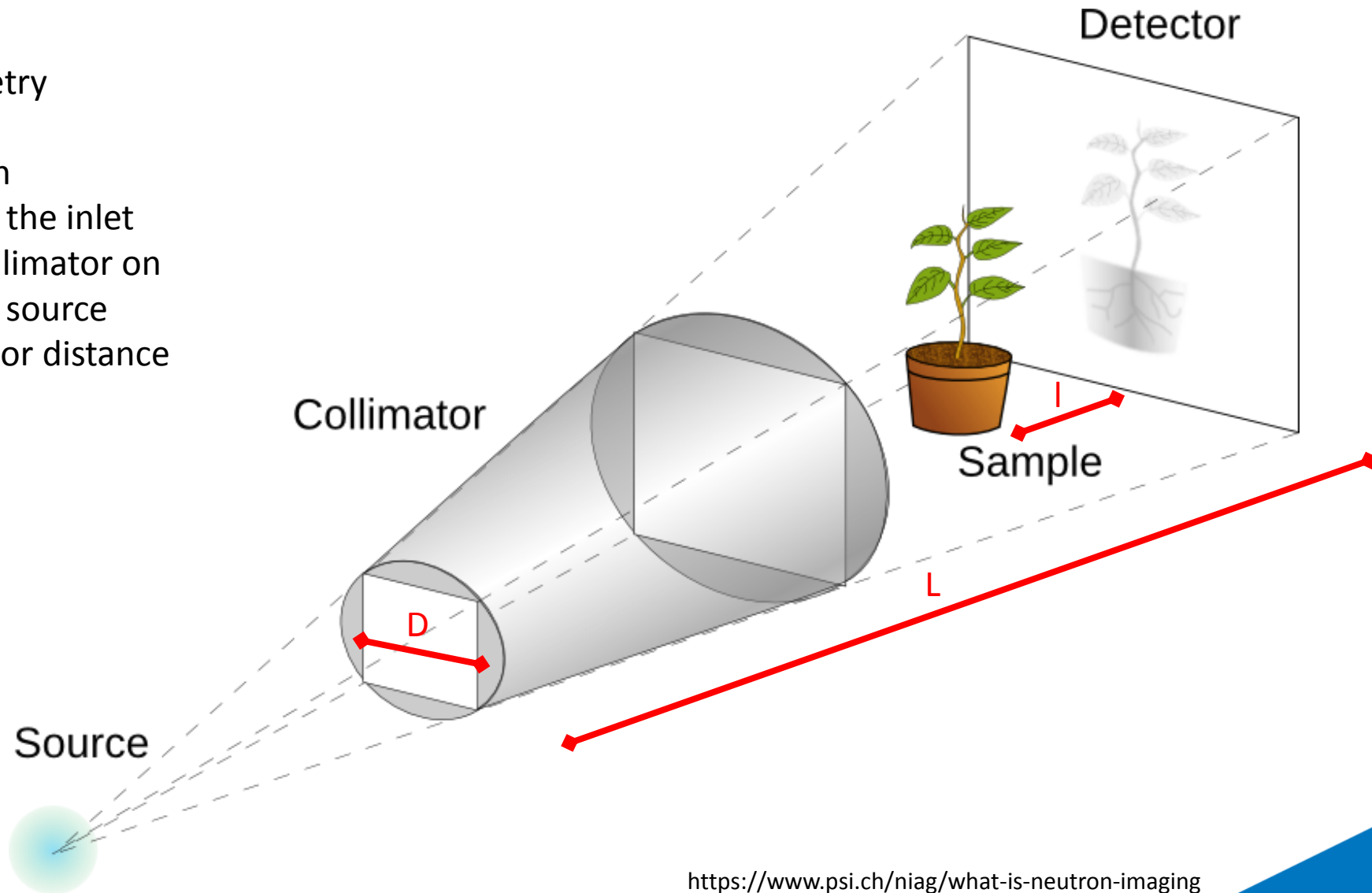
Collimation geometry

L/D

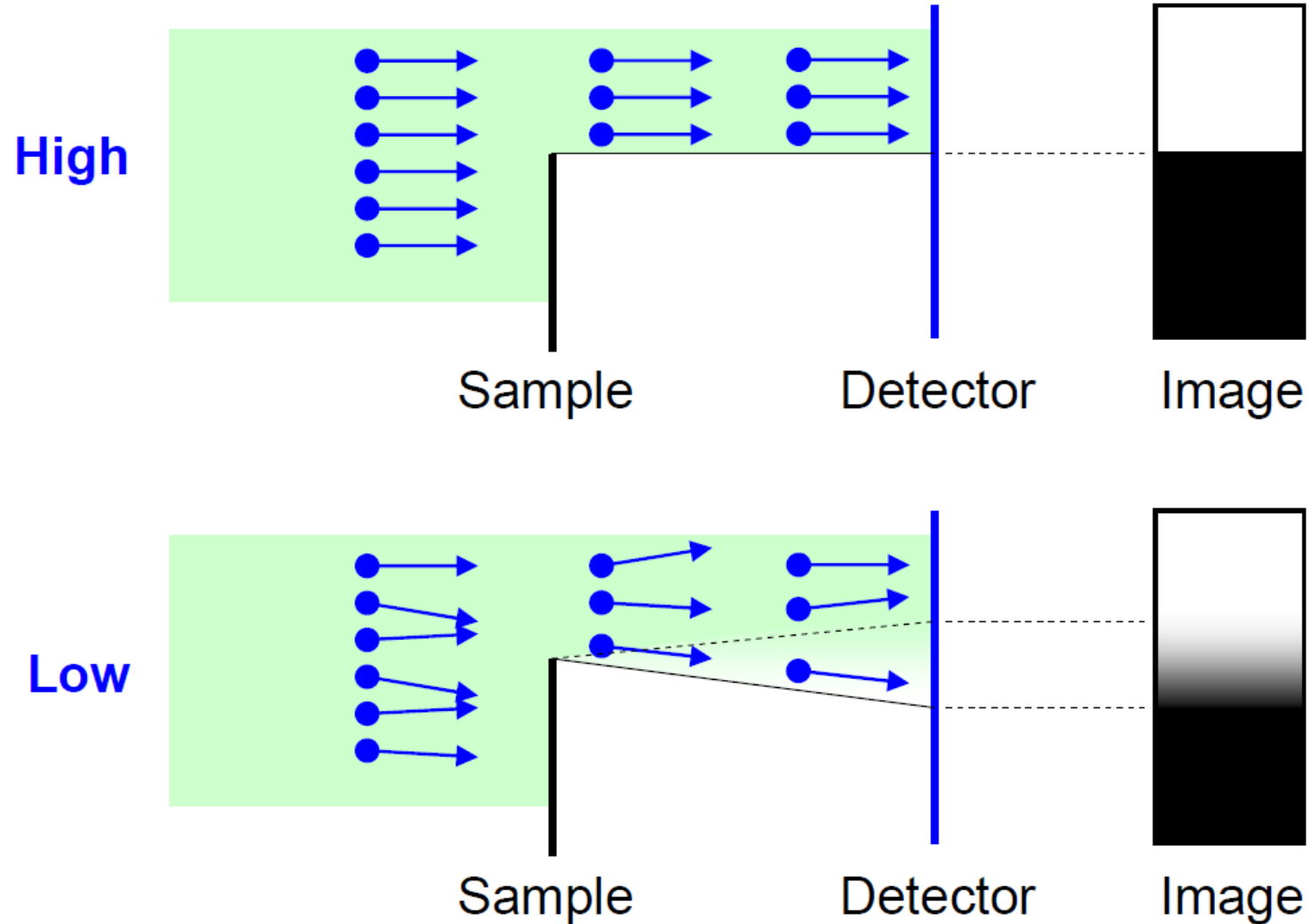
L: collimator length

D: the diameter of the inlet aperture of the collimator on the side facing the source

l: sample to detector distance

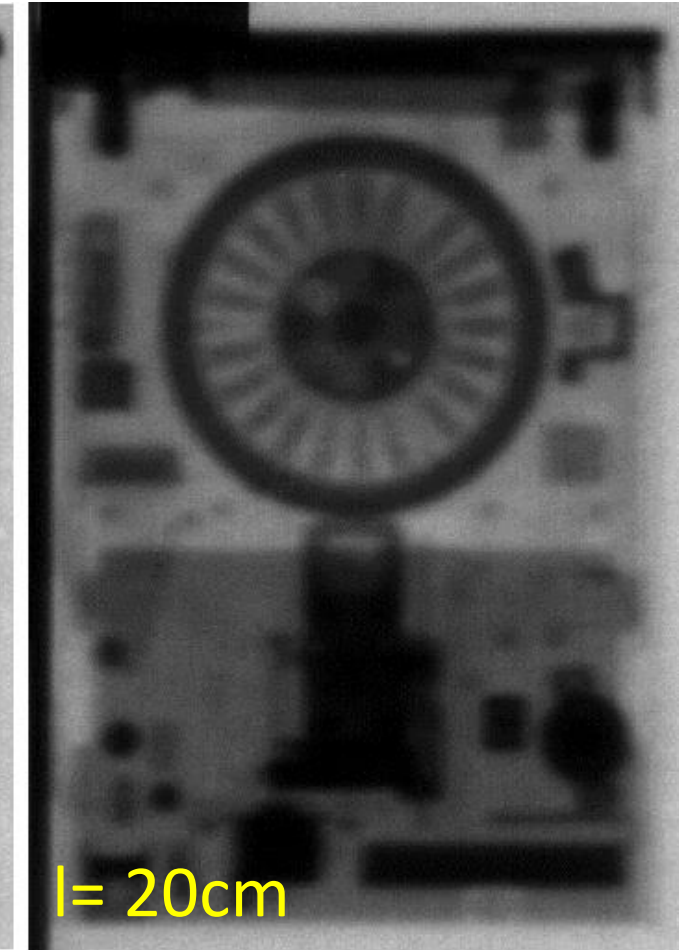
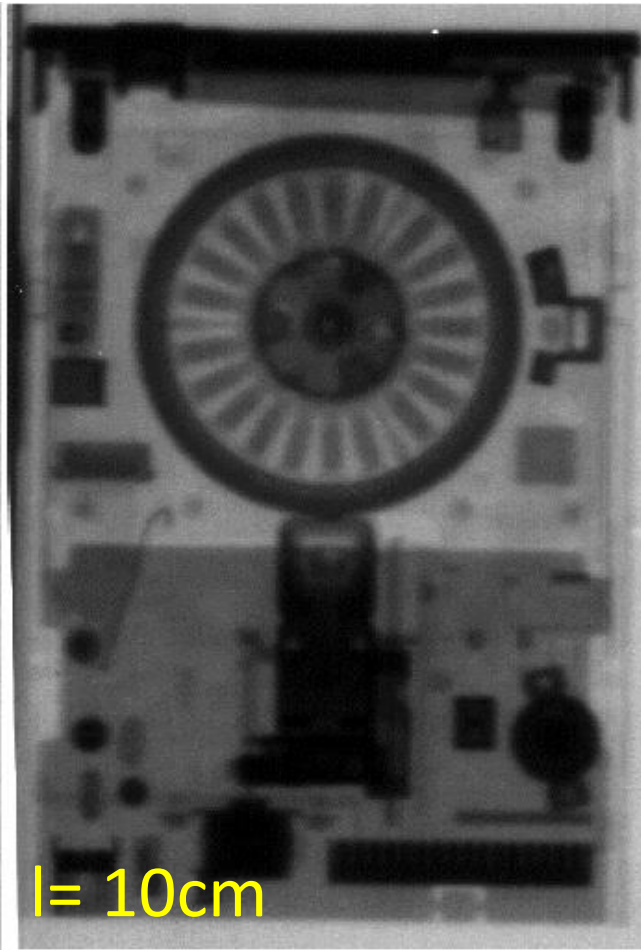
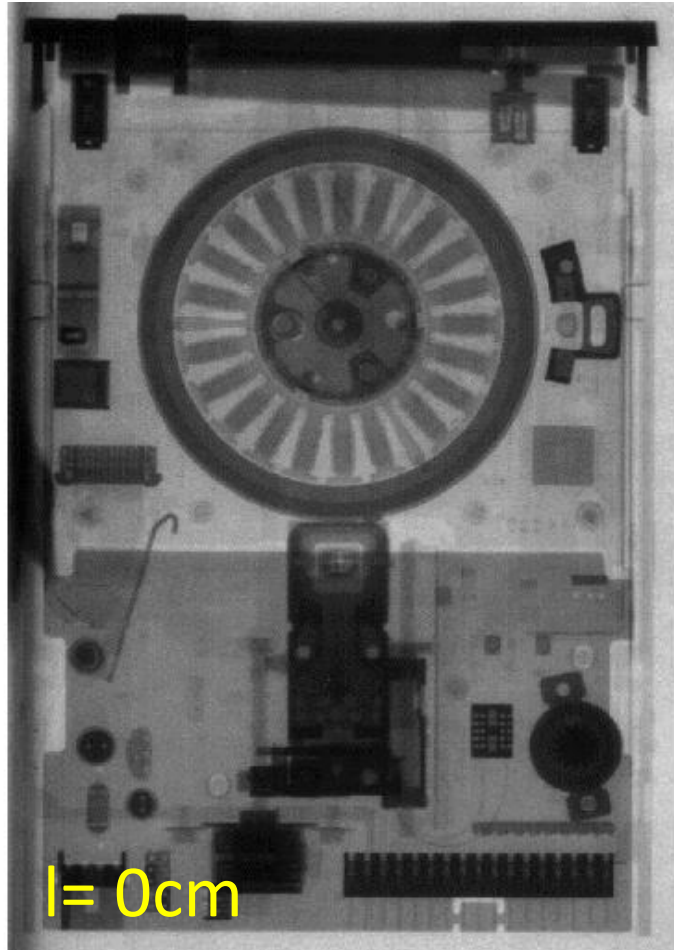


Effect of L/D on resolution

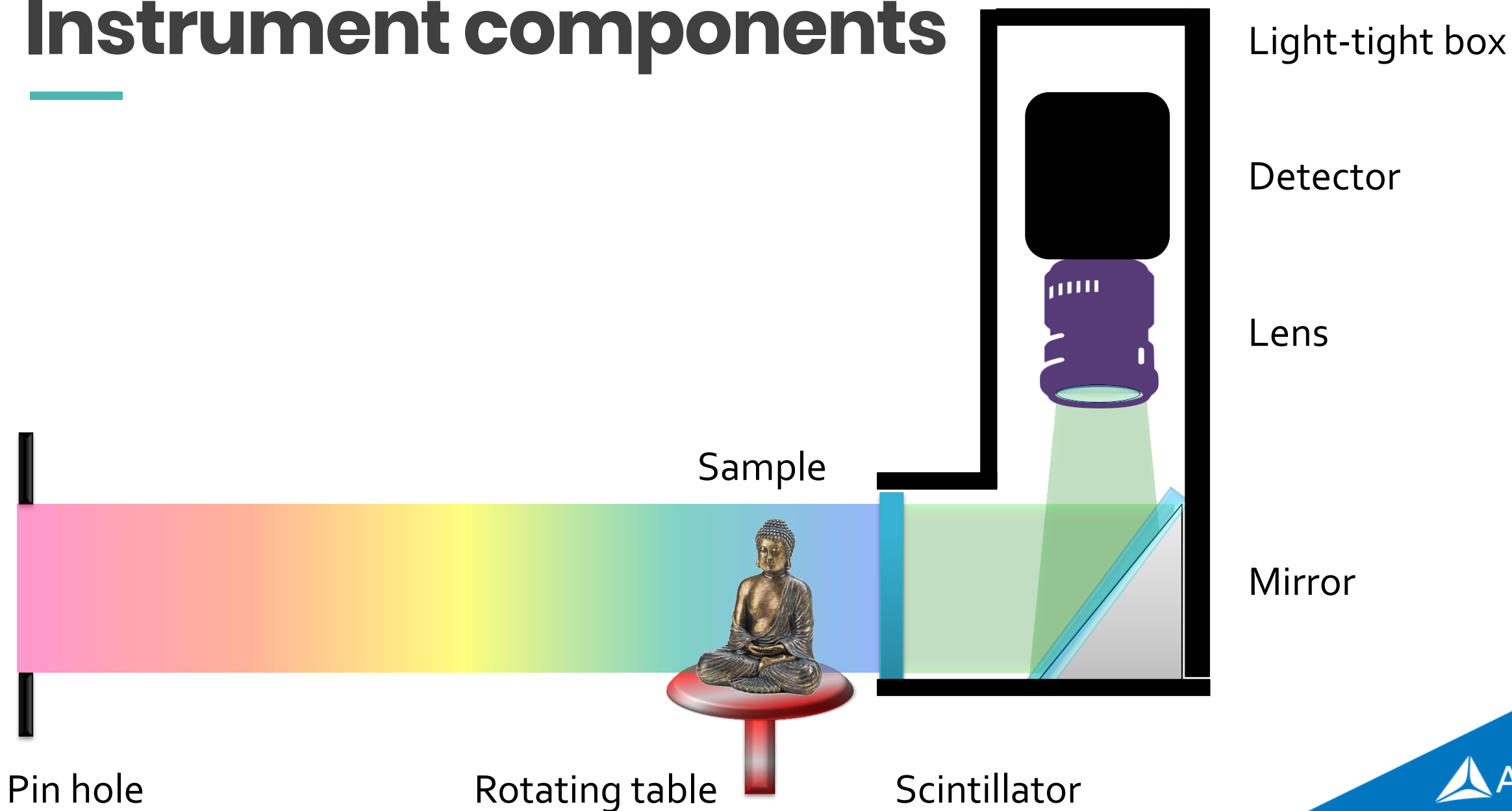


Effect of l on resolution

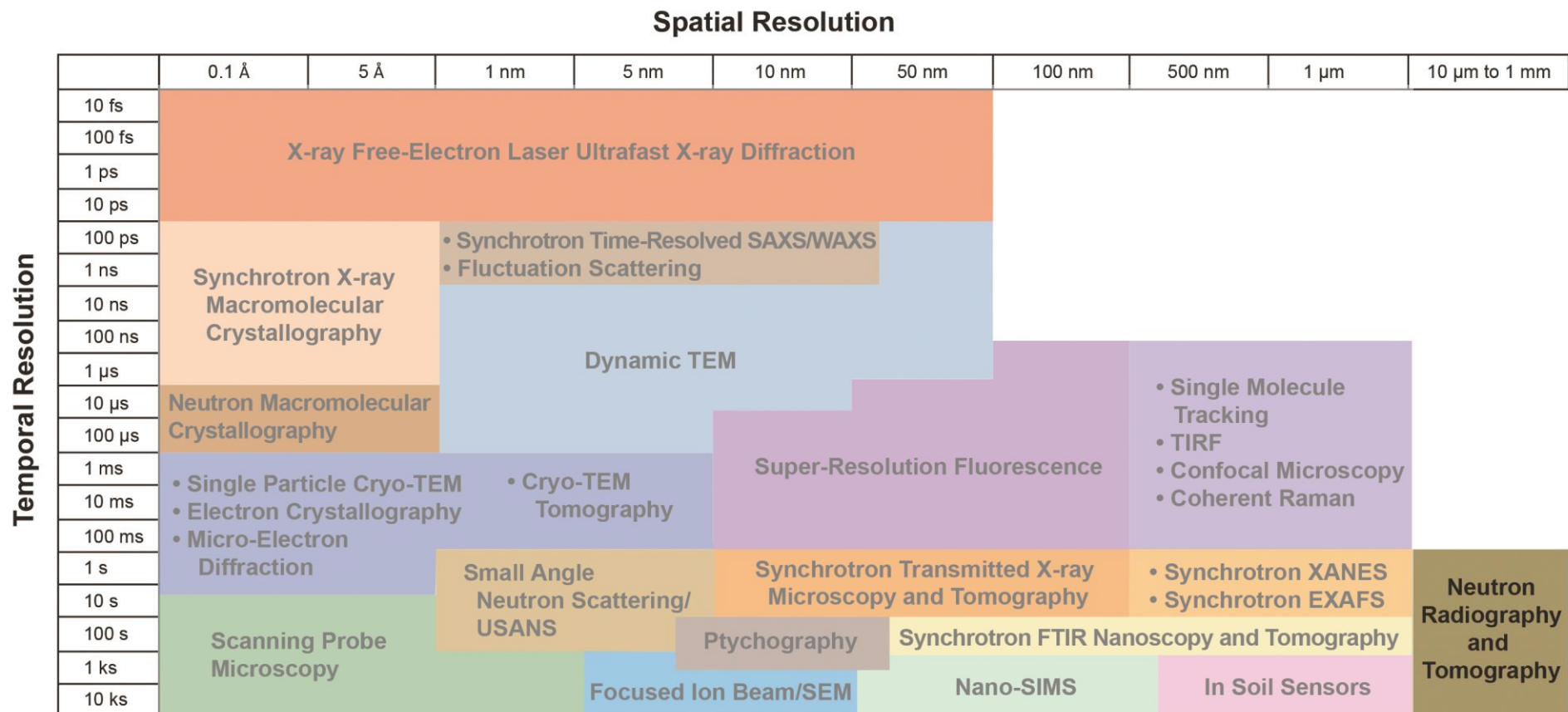
$L/D=71$



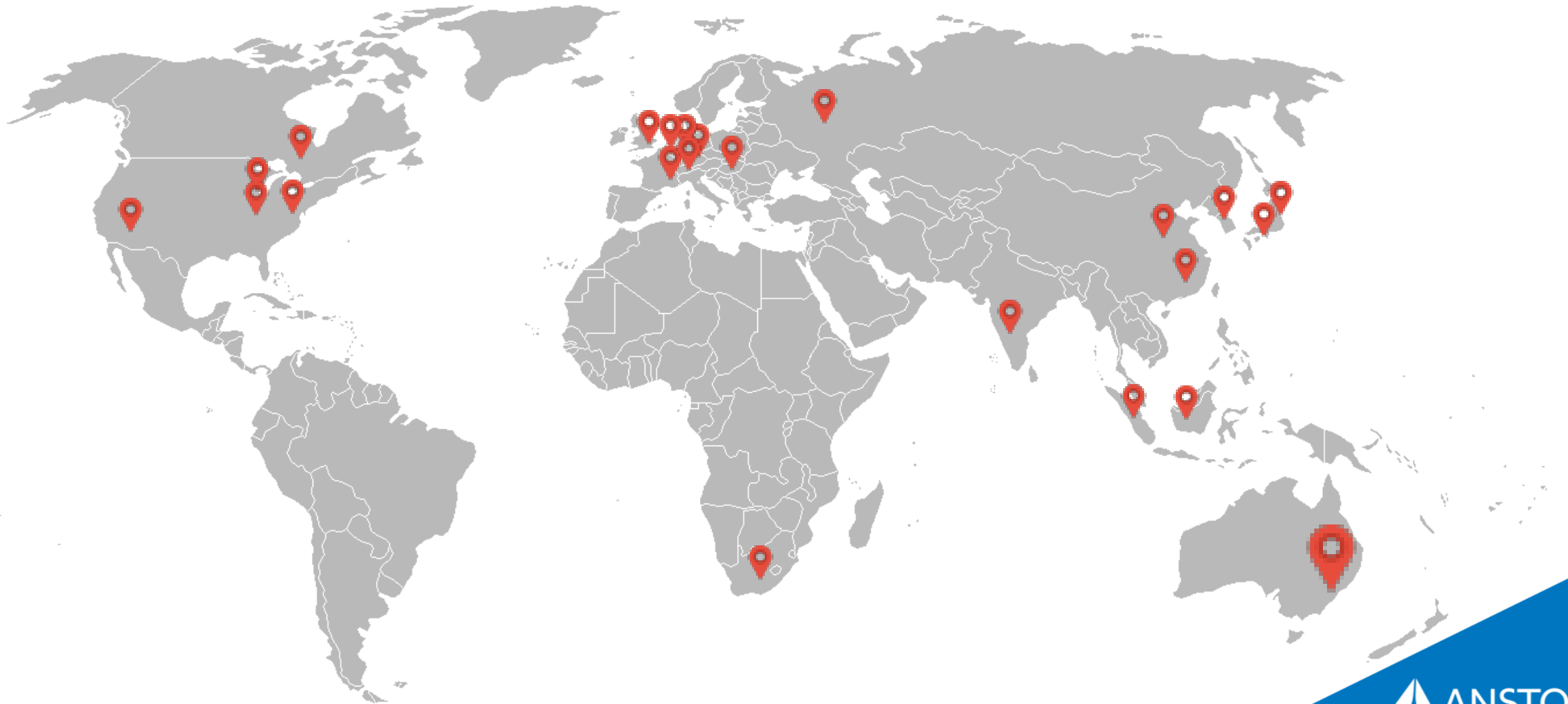
Instrument components



Spatial and Temporal Resolutions of Imaging Technologies



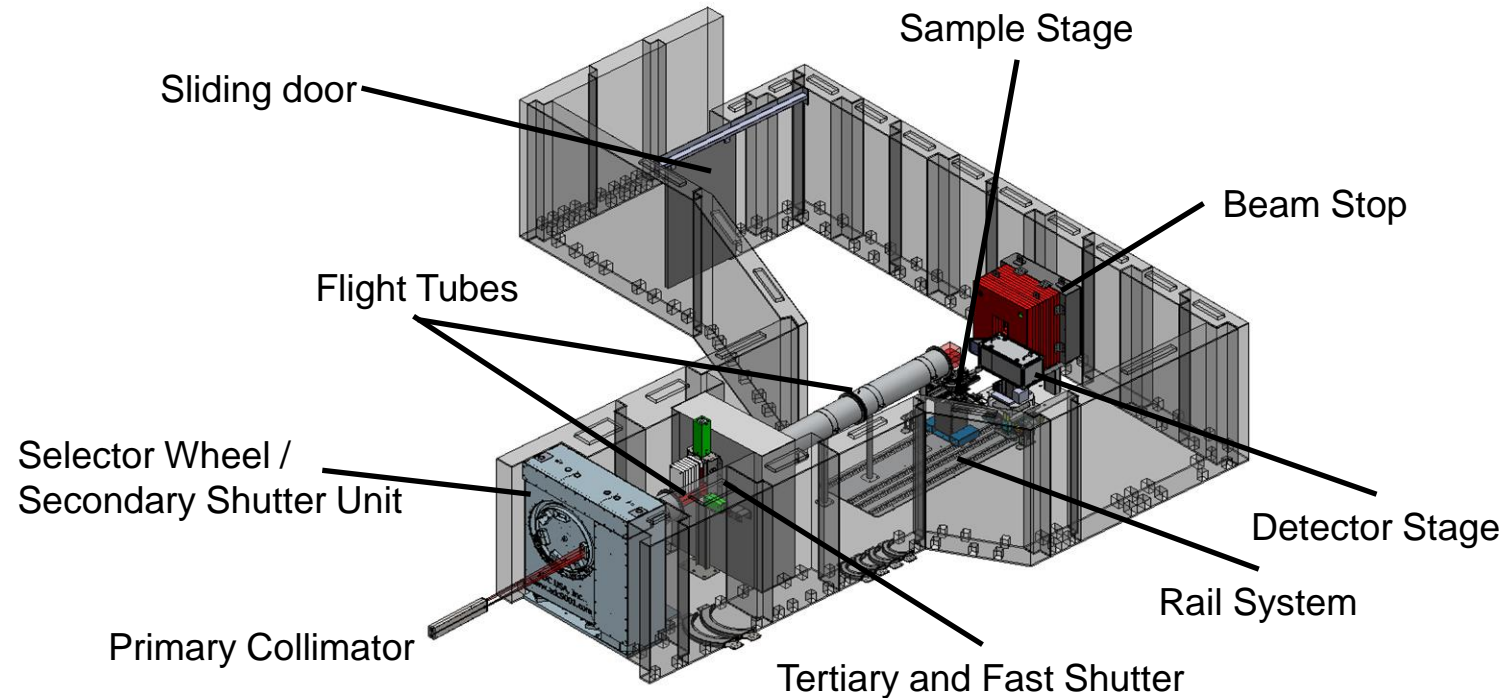
Neutron Imaging beamline in the world



The neutron imaging beamline DINGO



DINGO specs

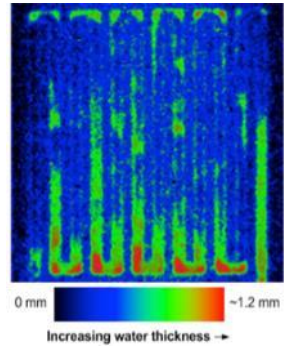
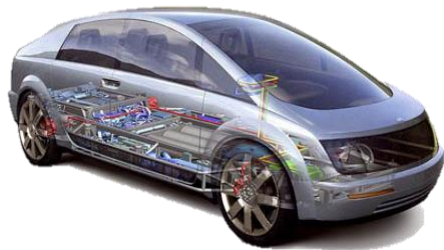


Technical details

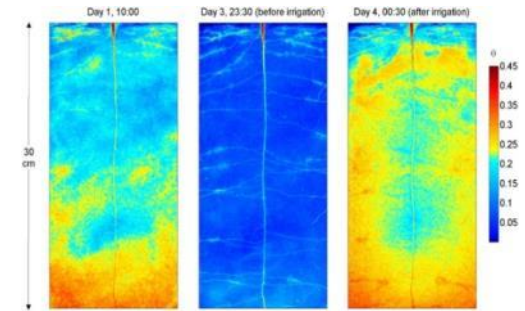
- Ikon-I CCD, NEO CMOS camera
 - Two Zeiss macro lens (50mm and 100mm)
- Three beam sizes 200 x 200, 100 x 100 and 50 x 50 mm²
 - Pixel size 10 – 100 μm
- 25fps fast imaging under development

Applications overview

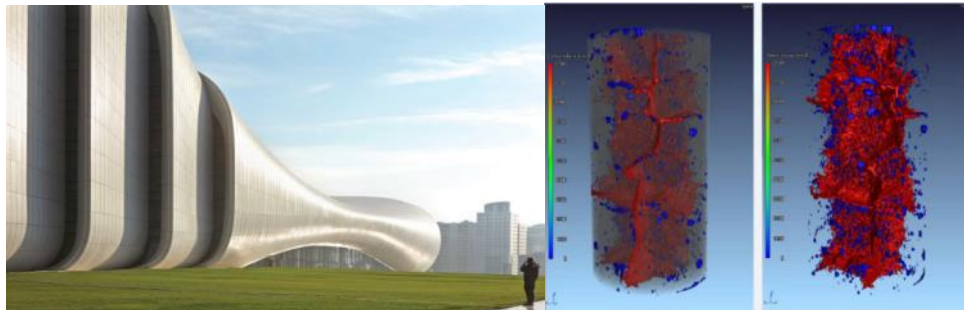
Energy



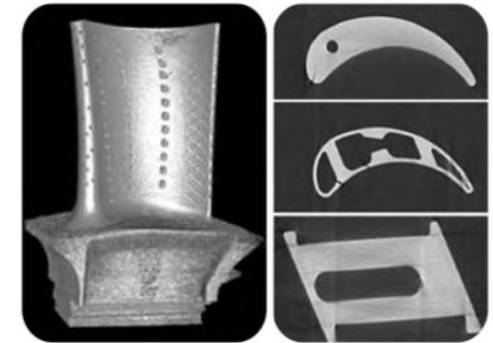
Agriculture & Food



Civil engineering



Industrial manufacturing



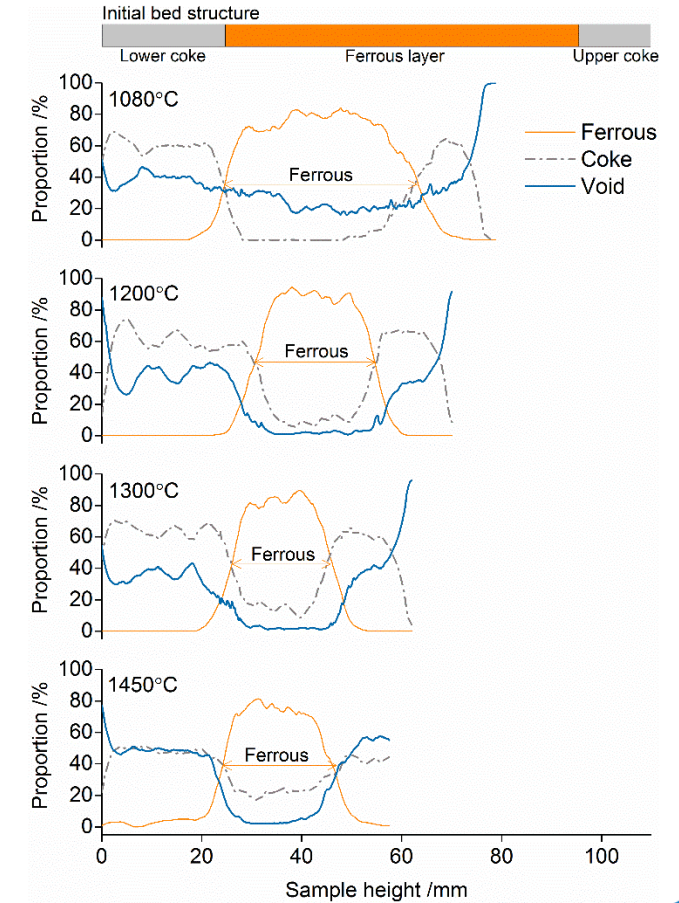
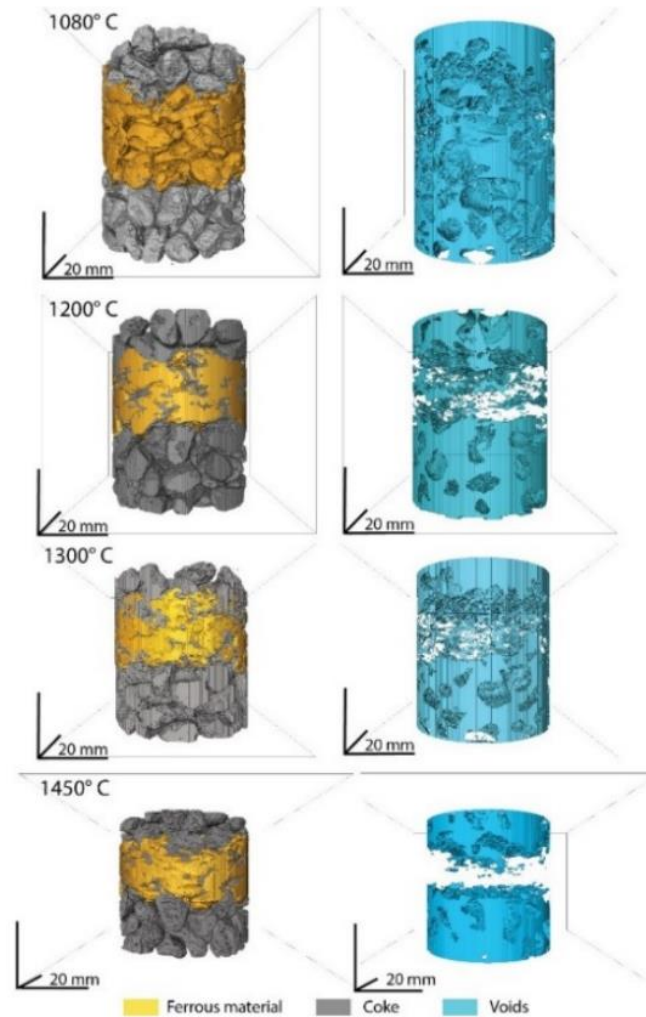
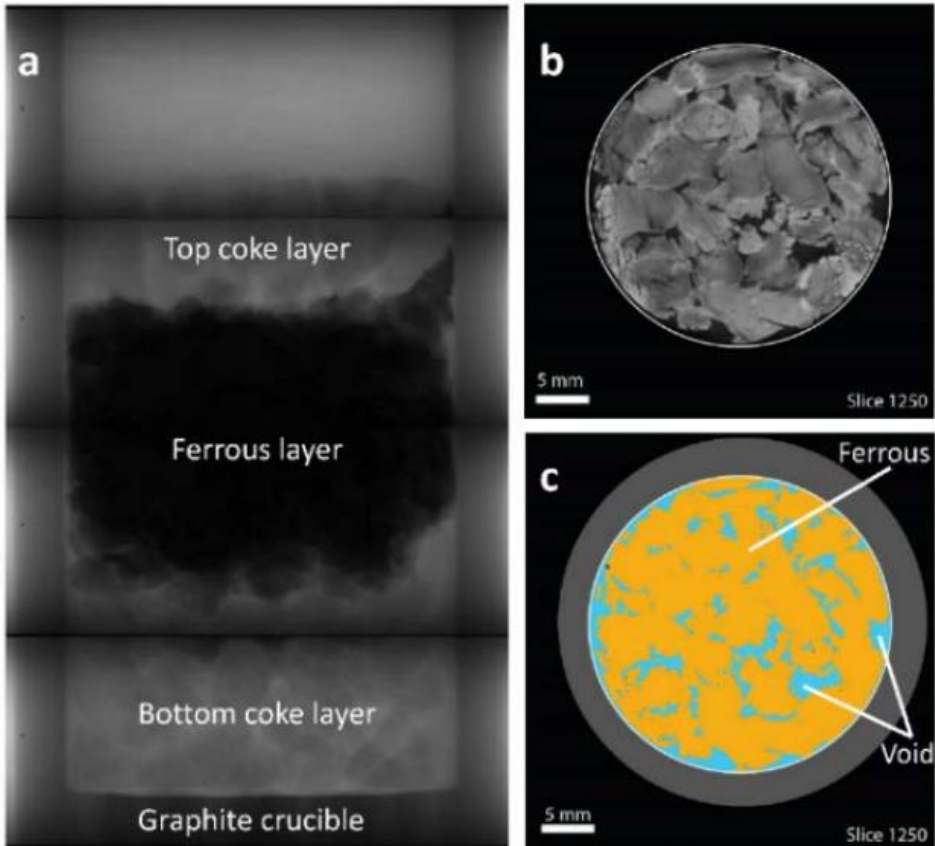
Earth & Planetary Science



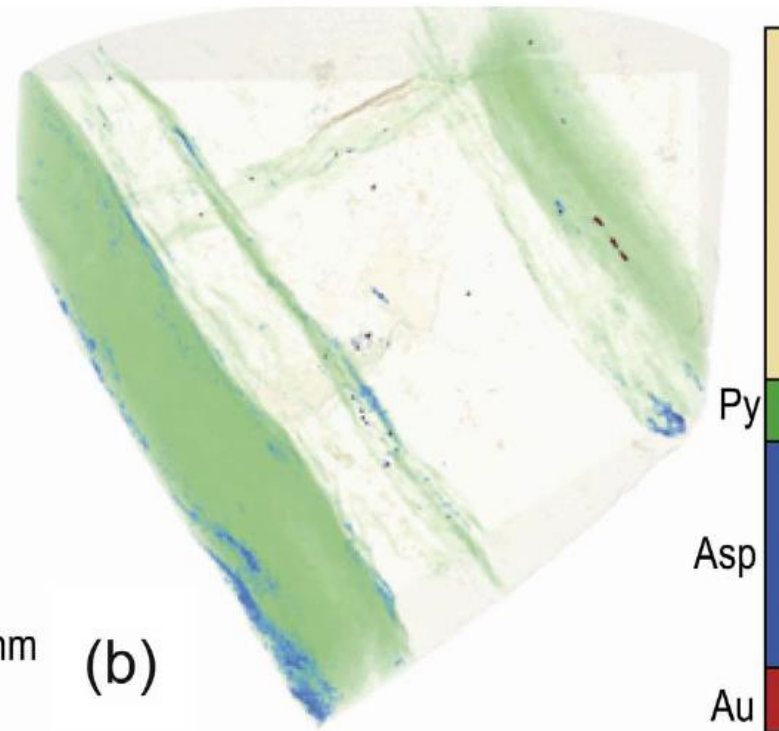
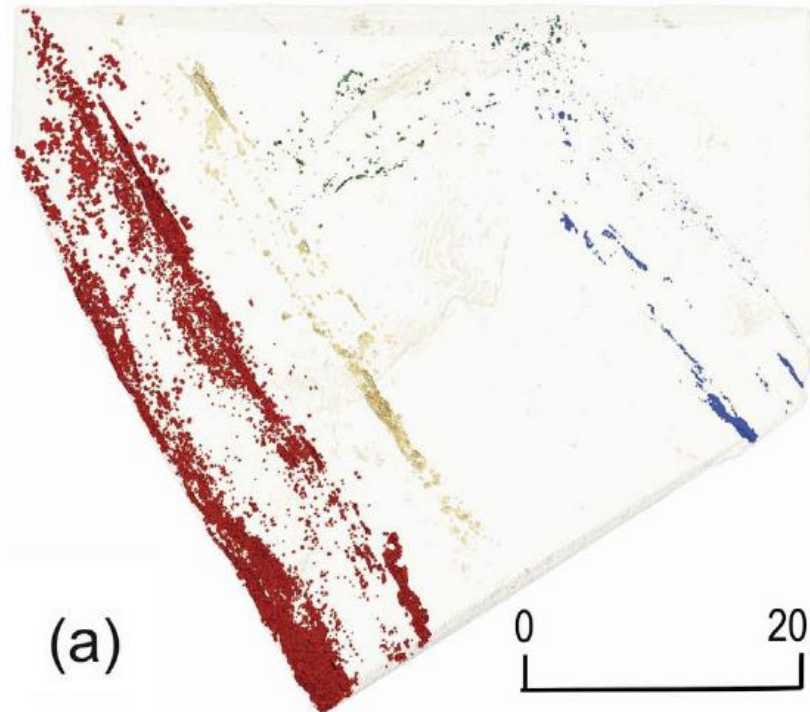
Biology and Medicine



Novel Measurement of Bed Voidage in Softening and Melting under Load Test



Costerfield antimony-gold deposit, southeast Australia: Coupling between brittle deformation and dissolution-precipitation reactions in the Melbourne Zone

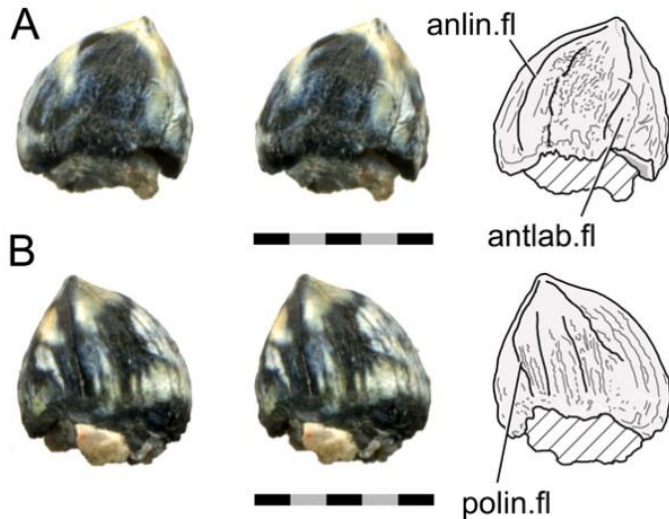
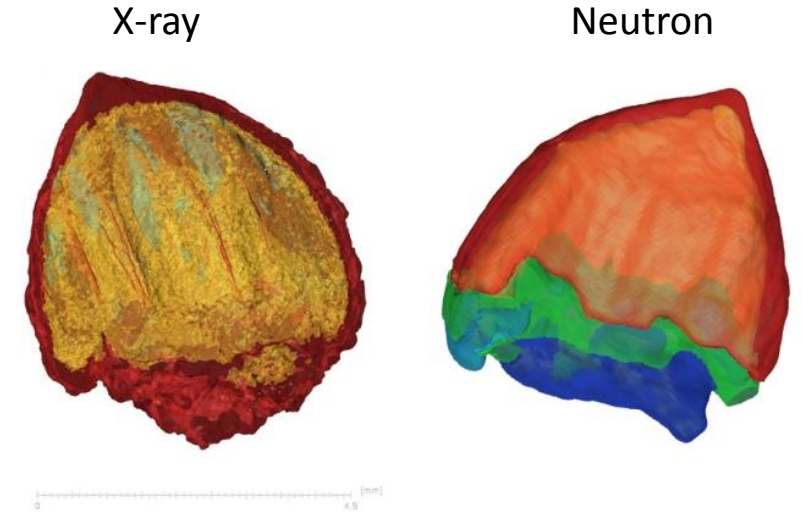
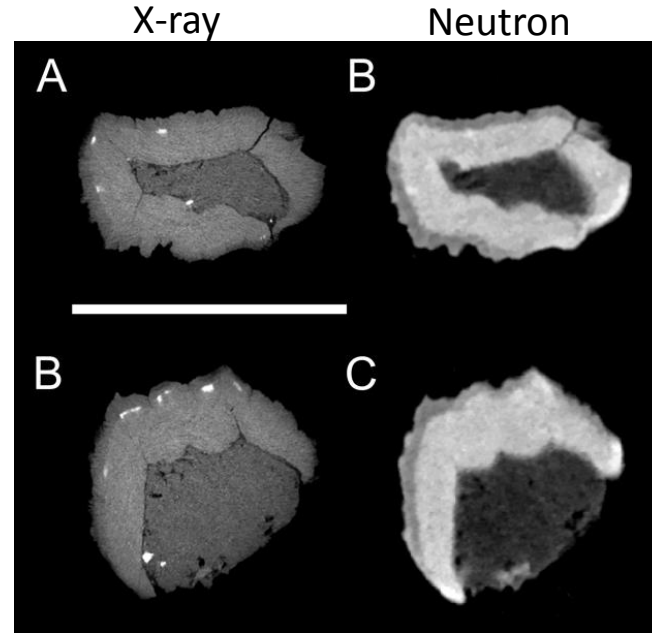


Phase	Composition	Σ [cm^{-1}] at 1.08 Å	Colour code
stibnite	Sb_2S_3	0.14	attenuation coefficient Σ [cm^{-1}]
galena	PbS	0.19	
antimony	Sb	0.23	
sphalerite	$(\text{Zn}, \text{Fe})\text{S}$	0.26	
quartz	SiO_2	0.28	
pyrite	FeS_2	0.40	
muscovite	$\text{KAl}_2(\text{Si}_3\text{Al})\text{O}_{10}(\text{OH}, \text{F})_2$	0.82	
biotite	$\text{K}(\text{Mg}, \text{Fe}^{++})_3[\text{AlSi}_3\text{O}_{10}(\text{OH}, \text{F})_2]$	0.85	
arsenopyrite	FeAsS	0.95	
gold	Au	3.95	

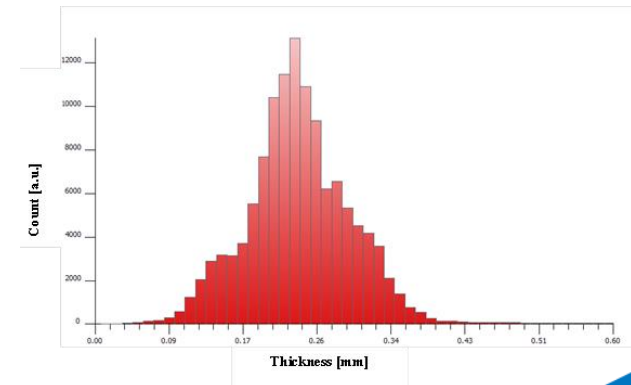
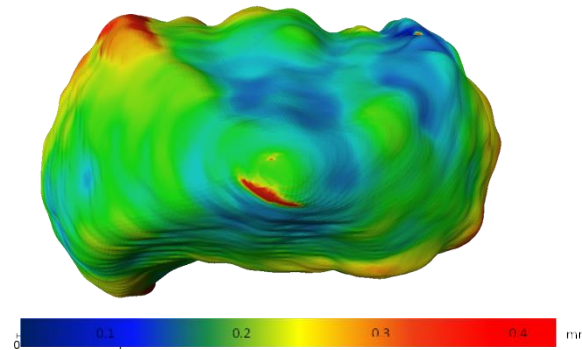
Neutron scanning reveals unexpected complexity in the enamel thickness of an herbivorous Jurassic reptile



Eilenodon (Rhynchocephalia)
Jurassic Morrison formation
North America



Neutron 3D map of enamel thickness



Final remarks

Neutron Imaging techniques as a tool to investigate matters

Technical advantages

- From micro- to macro- scale
- Bulk measurements
- Experiment can be designed

Materials

- Metals
- Ceramics
- Fossils
- Organic materials
-

Typical Investigations

- Documentation
- Identification of defects and inclusion
- Structural and Morphological bulk analysis
- Characterization of manufacturing technology
- Quality control
-

Outcome

- Statistical analysis
- Spatial map
- 3-D rendering and visual inspection
- Surface and mesh generation
- Modelling and simulation
-

Thank you